

<<椭圆函数>>

图书基本信息

书名：<<椭圆函数>>

13位ISBN编号：9787506265508

10位ISBN编号：7506265508

出版时间：2003-11

出版时间：北京世界图书出版公司

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页数：326

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内容概要

Elliptic functions parametrize elliptic curves, and the intermingling of the analytic and algebraic-arithmic theory has been at the center of mathematics since the early part of the nineteenth century. Some new techniques and outlooks have recently appeared on these old subjects, continuing in the tradition of Kronecker, Weber, Fricke, Hasse, Deuring. Shimura's book Introduction to the arithmetic theory of automorphic functions is a splendid modern reference, which I found very helpful myself to learn some aspects of elliptic curves. It emphasizes the direction of the Hasse-Weil zeta function, Hecke operators, and the generalizations due to him to the higher dimensional case (abelian varieties, curves of higher genus coming from an arithmetic group operating on the upper half plane, bounded symmetric domains with a discrete arithmetic group whose quotient is algebraic). I refer the interested reader to his book and the bibliography therein.

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